Introduction LR distributions and ROC curves for 10, 15, 23 loci Top-k probabilities Probability of exceeding LR thresholds Finding distant relatives Conclusions

Kinship testing with with (many) more markers

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Finding a relative among database profiles



Figure: Bieber et al. (2006) [1]

- Offender's profile is available, but yields no match in the database. Maybe a close relative is in the database?
- Procedure: compute LR in favor of a full sibling or parent/offspring relationship for all database members and further investigate a candidate list of 'large' LRs (say > 1,000)
- Exclude false leads by additional (genetic) research (mostly Y-STRs)
- Currently: limited power and many false leads to eliminate



Two strategies for selecting a candidate list

A search strategy strikes a balance between the power to detect a true relative and the workload (number of false leads to be eliminated)

Top-*k*

- Investigate a candidate list of fixed length
- In California, a list of 168 candidates is further investigated [2]

Fixed threshold

- Investigate LRs exceeding a threshold, e.g. Netherlands Forensic Institute
- A fixed threshold is optimal in the long run [3]



LR distributions: full siblings and unrelated

Conclusions

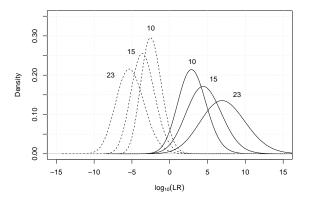


Figure: LR distributions for true full siblings (solid curves) and unrelated persons (dashed curves) for 10, 15 and 23 loci

ROC curve: full siblings and unrelated

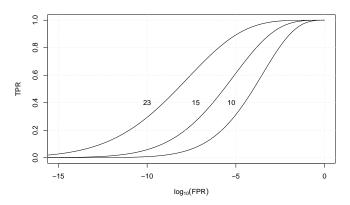


Figure: ROC curve: TPR (exceedance probability for a true relative) versus FPR (exceedance probability for an unrelated profile)



LR distributions: parents/offspring and unrelated

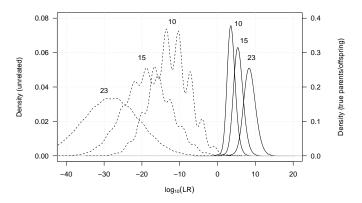


Figure: LR distributions for true parents/offspring (solid curves) and unrelated persons (dashed curves) for 10, 15 and 23 loci



ROC curve: parents/offspring and unrelated

Conclusions

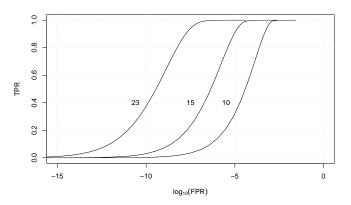


Figure: ROC curve: TPR (exceedance probability for a true relative) versus FPR (exceedance probability for an unrelated profile)



Relative identification (23 loci) versus direct matching

Conclusions

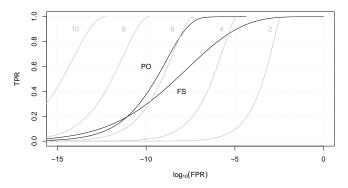


Figure: ROC curves for discrimination between first degree relatives and unrelated pairs using 23 loci (black curves) compared to those for direct identification using 2, 4, 6, 8, 10 ind. copies of D8S1179 (gray curves)

Top-k probabilities for full sibs in a 1M database

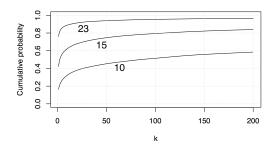


Figure: Probability for a true full sibling to appear in the top-k for a database of one million unrelated profiles for the three multiplexes

Top-k probabilities for parents/offspring in a 1M database

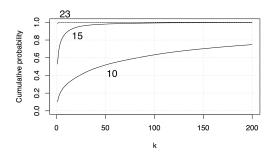


Figure: Probability for a true parent/offspring to appear in the top-k for a database of one million unrelated profiles for the three multiplexes

Top-k probabilities for full siblings

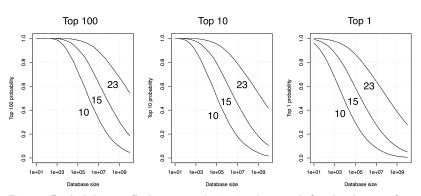


Figure: Probability to find a true relative in the top-k for databases of different sizes

Top-k probabilities for parents/offspring

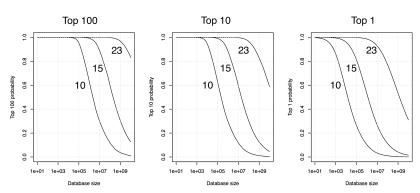


Figure: Probability to find a true relative in the top-k for databases of different sizes

LR > 1,000

		True relationship				
LR	# loci	PO	FS	HS	UN	
PO vs UN	10	7.48e-01	2.57e-01	3.57e-02	1.73e-04	
PO vs UN	15	9.85e-01	2.88e-01	2.50e-02	3.10e-05	
PO vs UN	23	9.99e-01	3.40e-01	1.71e-02	1.11e-06	
FS vs UN	10	3.37e-01	4.97e-01	2.97e-02	8.95e-05	
FS vs UN	15	7.22e-01	7.56e-01	6.40e-02	6.71e-05	
FS vs UN	23	9.69e-01	9.29e-01	1.28e-01	2.74e-05	

Table: Exceedance probabilities for LR > 1,000 for different choices of H_p , different true relationships and different number of loci



LR > 1,000,000

		True relationship			
LR	# loci	РО	FS	UN	
PO vs UN	10	2.03e-02	1.37e-02	8.47e-09	
PO vs UN	15	3.29e-01	9.35e-02	9.81e-08	
PO vs UN	23	9.59e-01	1.65e-01	4.44e-08	
FS vs UN	10	8.06e-03	5.71e-02	1.79e-08	
FS vs UN	15	8.85e-02	2.71e-01	5.22e-08	
FS vs UN	23	5.02e-01	6.51e-01	5.73e-08	

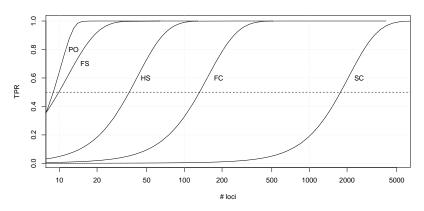
Table: Exceedance probabilities for LR > 1,000,000 for different choices of H_p , different true relationships and different number of loci



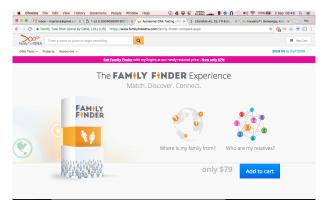
How many independent loci would be needed?

- A familial search to be feasible if there is a reasonable probability (say 50%) to detect a true relative (if present) at a reasonably small FPR (say 10^{-4})
- We investigate how many independent loci are needed for a familial search to be feasible for common pairwise relationships (FS, PO, HS, FC, SC)
- \bullet Procedure: find for each number of loci the LR threshold such that FPR = 10^{-4} and compute the corresponding TPR

How many independent loci would be needed?

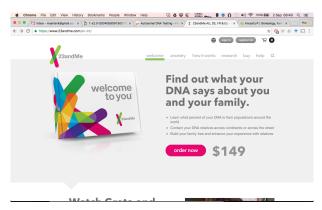


Who's on top?



Figure

Who's on top?



Figure

Who's on top?



Figure

Conclusions

- Since DNA databases profiles comprise just 10-15 loci, familial searches have limited power, are only suited for finding first degree relatives and it requires significant effort to eliminate false leads
- With 23 loci, finding first degree relatives is possible without the need to eliminate many false leads
- Familial searches for full siblings will become feasible in larger databases (e.g. United States NDIS)
- A parent/offspring search will be practically match/no match
- Searching second degree relatives, on the other hand, remains problematic, even if many more markers would be included



References I



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